**ABSTRACT**

The ongoing competition between bus and railway systems in the Hungarian regional passenger transport is a current problem, because these subsectors need to complement each other, instead of being in the government-funded competition. Long-term sustainability and efficiency in passenger transport require a balanced transport policy. The parallel bus and railway links, which are present in all regions of Hungary can result in competition. This research explores the solutions to this issue for long-term environmental and economic sustainability optimization. An objective index and interventions developed in previous studies have been applied here. This investigation is to validate the objective index and the interventions by using the Logit model.

**KEY WORDS**

parallel public transport system; logit model; mode choice; quality index; weighted coefficient;

1. INTRODUCTION

Public transport plays a significant role in the people’s lives in Hungary, also affecting the national economy. Therefore, its development is essential for long-term environmental and economic sustainability [1]. Even though there is constant innovation, thanks to both governmental and EU subsidies, the necessary macroscopic traffic organizational tasks remain marginalized.

From the government point of view, the long-term solution would be a market-based, non-state-subsidized passenger transport service. However, the decree regulation (EC) No. 1370/2007 of the European Parliament states that “[…] currently multiple countryside passenger transport services meet the needs of general economic interest, therefore cannot be operated on a commercial basis”.

The modal split between transport subsectors was researched in Hungary by Farkas, Hagymási and Nagy [2], as well as Ács [3], whose investigations concern the comparative analysis of subsectors. Internationally, Abramović, Zitricky and Mesko [4], Abramović [5], Droździel et al. [6], Gašparik, Abramović and Zitrický [7], Gašparik, Mesko and Zahumenska [8], Zitrický, Černá and Abramović [9], Kuang et al. [10], Llano et al. [11], van der Weijde et al. [12] investigated this topic. Albert and Tóth [13] discussed this topic in a more detailed manner, arriving at an index number which gives results from the operator’s aspect. Zhu et al. [14] studied the problem from the management’s point of view.

To fill the gap of international research, in previous studies of Lakatos and Mándoki [15], [16] a new quality index number \((M)\) was calculated (Equation 1) – regarding the parallel service links in Figure 1 – based on some of the critical factors which include: the number of inhabitants to be served, public transport availability, and efficiency in time of travel for vehicles and passengers.

\[
M = \sum_{j=1}^{J} \left( \frac{1}{n_{day,i,j,b}} \cdot \ln(\text{avail})_{i,j,b} \cdot p_j \cdot \frac{1}{n_{day,i,j,v}} \cdot \ln(\text{avail})_{i,j,v} \cdot p_j \right)
\]

where:

- \(i\) – settlement of departure;
- \(j\) – serial number of destination settlement;
- \(b\) or \(v\) – examined transport mode (bus (b) or train (v));
- \(n_{day,i,j,b}\) – daily supply in two directions in the case of bus service between each settlement served by the examined links [departures/day];
The purpose of this paper is to analytically validate the borders of intervals in the quality index number function (Figure 2). For the travel links depicted in Figure 1, the weighted coefficients of mode choice depending on the values of quality index number are to be determined, based on logistic regression (logit model) – as a mathematical tool – and on the number of passengers counted on the chosen parallel links. The functions of different weighted factors can be determined using the quality index number \(M\). An analysis of these functions and their extreme values on the borders of the intervals in Figure 2 are to be corrected.

The research framework is shown in Figure 3.

2. METHODOLOGY

The spatial and temporal distribution of trips is determined by the quality of the existing transport modes. The mode choice can be described by a probability model based on the spatial distribution of trips [17].

Two explanations of the Logit model (logistic regression) exist [18, 19]. The simpler and probably more popular formulation is a probability Equation 2:

\[
\text{logit}(y = 1) = \beta \cdot x
\]

where \(y\) is a discrete dependent variable (\(y=1\) is “success” \(y=0\) is “failure”), the logit function is the logarithm of the event chance in an argument, in turn, \(\beta \cdot x\) is a linear combination of the coefficient and the explanatory variable. The \(\beta\) coefficients are the parameters of logistic regression. Though on the right side there is no failure term, the stochastic connection between the observed output and the

---

**Table 1 – Value of the quality index \(M\) for each examined parallel link [16]**

<table>
<thead>
<tr>
<th>Name of the parallel line</th>
<th>(M)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Kaposvár – Siófok</td>
<td>-19.29</td>
</tr>
<tr>
<td>Székesfehérvár – Komárom</td>
<td>-13.71</td>
</tr>
<tr>
<td>Nyíregyháza – Vásárosnamény</td>
<td>-1.68</td>
</tr>
<tr>
<td>Zalaegerszeg – Rédcas</td>
<td>-5.0</td>
</tr>
<tr>
<td>Szeged – Békéscsaba</td>
<td>-0.29</td>
</tr>
<tr>
<td>Budapest – Kunszentmiklós</td>
<td>2.03</td>
</tr>
<tr>
<td>Debrecen – Füzesabony</td>
<td>4.97</td>
</tr>
</tbody>
</table>
As Functions 2 and 3 define the same probability, the connection between the direct probability model $\beta$ coefficients and the latent coefficient-based linear regression model $\alpha$ coefficient describes Function 5:

$$
\beta = \frac{\alpha}{\sigma}
$$

In order for the attributions of each transport mode (in this case bus and railway) to be evaluated based on their weights, a utility function has to be determined for all of the choices, based on the linear combination of weight numbers attributes ($g_m$). The generic form of this utility function is given by:

$$
U(x_1, x_2, \ldots, x_n)
$$

In this case, two transport modes are examined (bus and railway), so the utility functions are, respectively:

$$
U_b = x_{11} \cdot g_1 + x_{12} \cdot g_2 + \ldots + x_{1n} \cdot g_n
$$

$$
U_r = x_{21} \cdot g_1 + x_{22} \cdot g_2 + \ldots + x_{2m} \cdot g_m
$$

where:

- $x_{nm}$ — evaluable attribute “$m$” in choice “$n$”;
- $g_m$ — attribute weight number;
- $U_b$ — utility function, which describes the bus transport system;
- $U_r$ — utility function, which describes the railway transport system.
When choosing a way of transport, the most frequent attributes are cost and time, which were calculated in a previous study [16] for the examined seven regional parallel links. These cost and time values are based on travels from city centres to city centres. Transforming Equations 7 and 8, the following utility functions can be defined:

\[ U_b = T_{b,ij} \cdot w_t,b + K_{b,ij} \cdot w_c,b \]  
\[ U_r = T_{r,ij} \cdot w_t,r + K_{r,ij} \cdot w_c,r \]  

where:

\( T_{b,ij} \) – value of travel time between settlements \( i \) and \( j \) using the bus transport system;
\( K_{b,ij} \) – value of travel cost between settlements \( i \) and \( j \) using the bus transport system;
\( w_{t,b} \) – weighted coefficient of travel time using the bus transport system;
\( w_{c,b} \) – weighted coefficient of travel cost using the bus transport system;
\( T_{v,ij} \) – value of travel time between settlements \( i \) and \( j \) using the railway system;
\( K_{v,ij} \) – value of travel cost between settlements \( i \) and \( j \) using the railway system;
\( w_{t,v} \) – weighted coefficient of travel time using the railway system;
\( w_{c,v} \) – weighted coefficient of travel cost using the railway system.

The utility function was calibrated based on literature data by Martinez, Aguila and Hurtubia [22], Tánczos and Török [23], Kosztyó and Török [24].

In each case, the probability of bus \( P_b \) and train \( P_r \) can be defined by the function values of \( U_b \) and \( U_r \), respectively:

\[ P_b = f(U_b, U_r) \]  
\[ P_r = f(U_b, U_r) \]  

Using a logit model to the binary case – mentioned above:

\[ P_{+1} = \frac{e^{U_{+1}}}{\sum_{a} e^{U_a}} = \frac{e^{U_{+1}}}{e^{U_{+1}} + e^{U_{-1}}} \]  
\[ P_b = \frac{e^{U_b}}{e^{U_b} + e^{U_r}} = \frac{e^{T_{b,ij} \cdot w_t,b + K_{b,ij} \cdot w_c,b}}{e^{T_{b,ij} \cdot w_t,b + K_{b,ij} \cdot w_c,b} + e^{T_{r,ij} \cdot w_t,r + K_{r,ij} \cdot w_c,r}} \]  
\[ P_r = \frac{e^{U_r}}{e^{U_b} + e^{U_r}} = \frac{e^{T_{r,ij} \cdot w_t,r + K_{r,ij} \cdot w_c,r}}{e^{T_{b,ij} \cdot w_t,b + K_{b,ij} \cdot w_c,b} + e^{T_{r,ij} \cdot w_t,r + K_{r,ij} \cdot w_c,r}} \]  

where: \( 0 \leq P_b \leq 1 \) and \( P_b + P_r = 1 \).

In the utility functions, the values of travel cost and travel times are known. The number of passengers was taken from the official national traffic measurement organized by KTI Institute for Transport Sciences in 2016 [21]. The observation-based probability values of \( \bar{P}_{b,ij} \) and \( \bar{P}_{r,ij} \) can be calculated:

\[ \bar{P}_{b,ij} = \frac{N_{b,ij}}{N_{b,ij} + N_{v,ij}} \]  
\[ \bar{P}_{r,ij} = \frac{N_{v,ij}}{N_{b,ij} + N_{v,ij}} \]  

where:

\( N_{b,ij} \) – number of passengers between settlements \( i \) and \( j \) based on national traffic measurement in the bus transport system;
\( N_{v,ij} \) – number of passengers between settlements \( i \) and \( j \) based on national traffic measurement in the railway system;
\( N_{b,ij} + N_{v,ij} \) – number of all passengers between settlements \( i \) and \( j \) based on national traffic measurement.

The values of weighted coefficients in the utility function are defined as the minimum of sum-failures of probabilities in logit model \( (P_b, P_r) \) and the probabilities based on the traffic measurement \( (\bar{P}_{b,ij}, \bar{P}_{r,ij}) \). The minimum value (Min.) can be calculated with residual sum of squares:

\[ \sum_{ij} (\bar{P}_{b,ij} - P_b)^2 \rightarrow \text{Min.} \]  
\[ \sum_{ij} (\bar{P}_{r,ij} - P_r)^2 \rightarrow \text{Min.} \]  

More particularly:

\[ \text{RSS} = \sum_{ij} \left( \bar{P}_{b,ij} \cdot \frac{e^{T_{b,ij} \cdot w_t,b + K_{b,ij} \cdot w_c,b}}{e^{T_{b,ij} \cdot w_t,b + K_{b,ij} \cdot w_c,b} + e^{T_{r,ij} \cdot w_t,r + K_{r,ij} \cdot w_c,r}} \right)^2 \rightarrow \text{Min.} \]  
\[ \text{RSS} = \sum_{ij} \left( \bar{P}_{r,ij} \cdot \frac{e^{T_{r,ij} \cdot w_t,r + K_{r,ij} \cdot w_c,r}}{e^{T_{b,ij} \cdot w_t,b + K_{b,ij} \cdot w_c,b} + e^{T_{r,ij} \cdot w_t,r + K_{r,ij} \cdot w_c,r}} \right)^2 \rightarrow \text{Min.} \]

To define the values of weighted coefficients in each relation more exactly, the calculations were made with MS Solver.

For each parallel link mentioned in Figure 1, the values of travel time and travel cost-weighted coefficients were calculated with Equations 20 and 21.

3. RESULTS

The calculated values of the weighted coefficients can be assigned to the values of quality index \( (M) \) of each parallel link (Table 2).

4. ANALYSIS AND DISCUSSION

It is important to emphasize that the suggested interventions [16] were set for reaching the highest travel time-weighted coefficients by a previous
in favour of the bus transport system in the number of passengers. The constant nature of the function in Figure 4 validates the interventions (Figure 2) because bus links can serve – with preferential travel time values – the commuting traffic. In the railway system a more significant investment (e.g. introducing electric railway links, re-planning track routes, increasing the speed, etc.) can be the solution. The high costs of such changes must be considered.

Railway links that belong to Interval No. 1 (Kaposvár – Siófok, Székesfehérvár – Komárom, Zalaegerszeg – Rédcisz) have the same characteristics; they serve rural areas with settlements having 100-1,000 inhabitants. The train stations are near the settlement’s border, and the supply is symbolical, too. On the opposite side, the bus service guarantees preferential, better values of travel time and bus stops are in the centres of the settlements.

In Interval No. 2 the cost function rises steeply, which changes the sign at quality index value -1.68. Because of this, the original border of intervals – based on previous research [16] – has to be refined from value -1 to -2. In the modified interval the effect of wt on mode choice permanently increases for those who choose the bus service, while the train is used decisively for its cost. The maximum difference between wt and wc is significant, ca. 0.6. Therefore, railway transport can be competitive only regarding

### Table 2 – Values of weighted coefficients in the function of values of the M quality index

<table>
<thead>
<tr>
<th>M [-]</th>
<th>Railway wt [-]</th>
<th>Railway wc [-]</th>
<th>Bus wt [-]</th>
<th>Bus wc [-]</th>
</tr>
</thead>
<tbody>
<tr>
<td>-19.29</td>
<td>0.486</td>
<td>0.514</td>
<td>0.486</td>
<td>0.514</td>
</tr>
<tr>
<td>-13.71</td>
<td>0.442</td>
<td>0.558</td>
<td>0.442</td>
<td>0.558</td>
</tr>
<tr>
<td>-5</td>
<td>0.426</td>
<td>0.574</td>
<td>0.426</td>
<td>0.574</td>
</tr>
<tr>
<td>-1.68</td>
<td>0.200</td>
<td>0.800</td>
<td>0.200</td>
<td>0.800</td>
</tr>
<tr>
<td>-0.29</td>
<td>0.521</td>
<td>0.479</td>
<td>0.521</td>
<td>0.479</td>
</tr>
<tr>
<td>2.03</td>
<td>0.300</td>
<td>0.700</td>
<td>0.300</td>
<td>0.700</td>
</tr>
<tr>
<td>4.97</td>
<td>0.539</td>
<td>0.461</td>
<td>0.539</td>
<td>0.461</td>
</tr>
</tbody>
</table>

Note: M, wt, wc were defined in Eq. (9) and (10) and in section Introduction.

![Figure 4](image-url)
the travel cost. The train stops should be optimized along the railway link to decrease the travel times. This change can result in increasing the quality index value, and thus increase the competitiveness of railway transport. Unused railway stops should be served by demand-responsive bus transport. The effect of stop optimization on competitiveness has already been used by the Finnish railway and in Hungary by the MÁV-HÉV company [26, 27].

Interval No. 3 should be divided into two parts based on Figures 4 and 5:

a) section between values -2 and 0;
b) section between values 0 and 2.

In section a) the rise of \( w_i \)-line for the bus service increases (ca. 51 degrees) and takes a negative value, while for the railway transport the opposite of this can be noticed, which results in a quick change. Close to the zero value of the quality index \( M \), the weighted coefficients of bus and railway are nearly equal; therefore, the travel time and the travel cost are equally crucial for the passengers, which results in competition.

The interval section b) shows a surprising result; namely, the bus system can efficiently serve the travel time, which weighted significantly for passengers in their mode choice. At the same time, it is essential to mention that the difference of the weighted travel time values is far lower (ca. 0.4) than the difference value in interval No. 2, and the rises of the functions are again ca. 40 degrees.

Considering the minor differences between sections a) and b), the suggested intervention should be the stop optimization of the railway link. If the approximation of the value of the weighted coefficients is beneficial, then the train stop optimization should be done on the train link. For example, the Szeged–Békéscsaba railway link and the corresponding parallel bus links belong to this category. They cover the areas with a higher population, guarantee the same supply (except between Szeged and Hódmezővásárhely). Furthermore, train and bus stops are located next to each other and near the city centre. This would decrease the travel time, and increase the service level of both transport modes by distributing the travel demand in time and space between the two public transport systems (e.g. parallel service only during rush hour, feeder bus links with railway-coordinated timetables in off-peak hours). Introducing business politically reduced fares (e.g. combined pass etc.) should also be considered. Parallel railway and bus links with the value of \( M \) between -2 and 2 cover the densely populated areas and connect high-populated cities by collecting people from different points of the settlements. Accordingly, both transport modes should operate, and their service level can be developed with some extra services (e.g. on-board Wi-Fi, modern vehicles, etc.) or with the more exact recognition of demand.

In Interval No. 4 the guaranteed weight number of travel time permanently shows a decreasing trend, while the railway function is increasing. It means that the services approach race condition, which is symbolized by the intersection of functions near the quality index value 5. To increase the travel time-based competitiveness of railway transport, stop optimization, and feeder bus system are needed. Unused railway stops should be served by demand-responsive bus transport.

In the case of No. 5, the bus systems function decreases until the endpoint (10.62 ~ 11), where it takes a constant value (0.01). Meanwhile, the railway transport function permanently increases until
maximum point on travel time values as a weighted coefficient, while passengers choose bus because of the travel costs.

As Figure 7 suggests, the interventions would cause advancement in the number of passengers using railways, because if the value of quality index $M$ is above zero, the number of transported passengers increases in the railway system, while below 0, the passengers tend to use buses.

It is important to mention that the commuter passengers (travelling a distance below 100 kilometres) choose the transport mode which guarantees the shortest travel time, as proved by [15].

The revised suggested interventions depending on the refined value of the quality index number are given in Figure 6.

In the course of previous research [16], parallel bus and railway links between Debrecen and Füzessabony were optimized based on the suggested interventions above and a Finnish example. Accordingly, the $M$ value advanced from 4.97 to 7.80. Applying the new value to Figures 4 and 5, it can be stated that the competition between the parallel links ceased, the function of the railway reached the maximum point on travel time values as a weighted coefficient, while passengers choose bus because of the travel costs.

As Figure 7 suggests, the interventions would cause advancement in the number of passengers using railways, because if the value of quality index $M$ is above zero, the number of transported passengers increases in the railway system, while below 0, the passengers tend to use buses.

It is important to mention that the commuter passengers (travelling a distance below 100 kilometres) choose the transport mode which guarantees the shortest travel time, as proved by [15].
5. CONCLUSION

This study aimed to support analytically the use of the objective index $M$ and interventions in the traffic system. For the verification, the values of travel time and travel costs, furthermore the number of passengers in each parallel bus and railway link – covering all the regions of Hungary – were evaluated with a logit model.

For both transport modes, the weighted travel time and travel cost values were calculated and assigned to the quality index number $M$. Consequently, the functions of weighted coefficients are reflected by the quality index intervals, which show the characteristics of competition between bus and railway systems.

If the value of quality index number is below -5, then the functions of the weighted coefficients are constant, and the bus system is chosen by most of the passengers because it guarantees shorter travel times. The high values of the function reflect this statement. In this case, the competitiveness of railway transport cannot be increased by only transport organization tools.

The functions of the weighted coefficients have ca. 45-degree slope between the value of quality index -5 and -1. In this interval the railway competitiveness can be increased by stop optimization. In interval -1 and +1 the lines change signs and their slopes approximate to competition point, which can be reached when the quality index number equals 0. As the slope of the lines changes the sign near the quality index number -2, the interval border determined by a previous study [16] has to be modified from -1 to -2.

There is a significant change near the quality index value +2. The function of the weighted coefficients according to the bus system has a slope with a negative value, while the function of the railway service shows the opposite trend, but the difference between the two functions is insignificant. Based on the statements above, the value of the internal border should be modified from +1 to +2.

Above the value of quality index number +5, the competition between the two transport modes disappears, the difference between the two functions permanently grows until value +10.62 (endpoint). From the endpoint, the functions reach the maximum and the minimum values (0.99 and 0.01). Above the mentioned point, it is not rational to aim at a higher quality index value, because functions have constant characteristics. Accordingly, the weight of the mode choice parameters is invariable.

A previous study [15] proved that for the passengers (ca. 80%) the travel time is the most important in their mode choice. Accordingly, to reach the highest value on the weighted coefficient lines in each quality index interval – considering the transport political aspects – the suggested interventions are relevant. Hungarian parallelism in regional public transport can be optimized by the created methodology and suggested interventions. This methodology can be used generally in every transport mode competition or to influence the public transport mode choice.

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A MAGYARORSZÁGI REGIONÁLIS PÁRHUZAMOS KÖZÖSSÉGI KÖZLEKEDÉSI RENDSZER ANALITIKUS, LOGIT-MODELL ALAPÚ VIZSGÁLATA

ABSZTRAKT

Az autóbusz- és vasúti közösségi közlekedési rendszerek között fennálló verseny a magyar regionális személyszállítási aktuális probléma, mivel ezeknek az aléghetőségének érdekében az államilag finanszírozott verseny helyett, a személyszállítás hosszú távú fenntarthatósága és hatékonysága kiegyensúlyozott közlekedéspolitikai körülményeket igényel. A párhuzamos busz- és vasútvonalak, amelyek Magyarország minden régiójában megjelennek, versenyhelyzetet eredményezhetnek. Ez a kutatás a fenti probléma megoldásait vizsgálja a hosszú távú környezeti és gazdasági fenntarthatóság érdekében, amelynek alapját egy korábbi tanulmányban kidolgozott objektív mutatószámok és azokhoz társított beavatkozások képezik. A magyar közlekedéshelyzetet és a beavatkozások befolyását a Logit-modell segítségével.

KULCSSZAVAK

módválasztás a közösségi közlekedésben; párhuzamos közlekedési kínálat; logit-modell;
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